

TABLE OF DERIVATIVES

FUNCTION	DERIVATIVE
C	0
cx	c
x^a	ax^{a-1}
	\leftarrow Multiply by current power. Add -1 to power.
$\sin x$	$\cos x$
$\cos x$	$-\sin x$
$\tan x$	$(\sec x)^2$
$\sec x$	$\sec x \tan x$
e^x	e^x
$\ln x $	$\frac{1}{x}$
a^x	$(\ln a)a^x$
$\log_b x$	$\frac{1}{(\ln b)x}$
$\sinh x$	$\cosh x$
$\cosh x$	$\sinh x$
$\tanh x$	$(\operatorname{sech} x)^2$
$\arcsin x$	$\frac{1}{\sqrt{1-x^2}}$
$\arccos x$	$\frac{-1}{\sqrt{1-x^2}}$
$\arctan x$	$\frac{1}{x^2+1}$
$\int_a^x f(t) dt$	$f(x)$

RULES FOR DERIVATIVES

Rule for addition:

$$\text{If } h(x) = f(x) + g(x) \quad \text{OR} \quad \frac{d}{dx}(u + v) = \frac{du}{dx} + \frac{dv}{dx}$$

Then $h'(x) = f'(x) + g'(x)$

Rule for scalar multiplication:

$$\text{If } h(x) = af(x) \quad \text{OR} \quad \frac{d}{dx}(au) = a \frac{du}{dx}$$

Then $h'(x) = af'(x)$

Product rule:

$$\text{If } h(x) = f(x)g(x) \quad \text{OR} \quad \frac{d}{dx}(uv) = \frac{du}{dx}v + u \frac{dv}{dx}$$

Then $h'(x) = f'(x)g(x) + f(x)g'(x)$

Quotient rule:

$$\text{If } h(x) = \frac{f(x)}{g(x)} \quad \text{OR} \quad \frac{d}{dx}\left(\frac{u}{v}\right) = \frac{\frac{du}{dx}v - u\frac{dv}{dx}}{v^2}$$

Then $h'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{(g(x))^2}$

Chain rule:

$$\text{If } h(x) = f(g(x)) \quad \text{OR} \quad \frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$$

Then $h'(x) = f'(g(x))g'(x)$